

Answer key, 2017

<p>1.  <math>3(x-1) - (x+9) = 0</math>  <math>3x - 3 - x - 9 = 0</math>  <math>2x = 12</math>  <math>x = 6</math></p>	<p>2.  <math>45_n = 41_{ten}</math>  <math>4 \times n^1 + 5n^0 = 4 \times 10^1 + 1 \times 10^0</math>  <math>4n + 5 = 41</math>  <math>4n = 36</math>  <math>n = 9</math></p>	<p>3.  <math>2x^3 = 54</math>  <math>x^3 = 27</math>  <math>x^3 = 3^3</math>  <math>x = 3</math></p>	<p>4.  <math>ab^2 - bc + ac</math>  <math>= 3(-2)^2 - (-2)(4) + (3)(4)</math>  <math>= 12 + 8 + 12</math>  <math>= 32</math></p>
<p>5. Let p be the loan, then <math>6000Frw = p \times \frac{24}{100}</math>  <math>p = \frac{6000 \times 100}{24}</math>  <math>= 2500Frw</math></p>	<p>6. the area of the trapezium is: <math>\frac{x(x+7+2x)}{2} = 24</math>  <math>x^2 + 7x + 2x^2 = 48</math>  <math>3x^2 + 7x - 48 = 0</math>  <math>3x - 9x + 16x - 48 = 0</math>  <math>3x(x-3) + 16(x-3) = 0</math>  <math>(3x+16)(x-3) = 0</math>  <math>3x = -16</math> or <math>x-3 = 0</math>  <math>x = \frac{16}{3}</math> (not valid) or <math>x = 3</math>  The value of <math>x = 3</math>cm</p>		
<p>7. Let the original number be x  Then <math>x \times \frac{180}{100} \times \frac{160}{100} = 144</math>  <math>x = 144 \times \frac{100}{180} \times \frac{100}{160}</math>  <math>x = 50</math></p>	<p>8. In triangle BCD, angle CBD = <math>90^\circ</math> (angle in a semicircle = <math>90^\circ</math>)  AB = AD (tangents from the same external point to the circle)  So triangle ABD is isosceles hence angle ABD = angle ADB  <math>= \frac{1}{2}(180 - 40)</math>  <math>= 70^\circ</math></p>		
<p>10. <math>y = \frac{k}{x}</math> then <math>xy = k</math>  <math>k = 3 \times 40</math>  <math>2.5y = 120</math>  <math>y = \frac{120}{2.5} = 48</math></p>	<p>11.  The sum of exterior angles of a polygon = <math>360^\circ</math>  So <math>y = 85^\circ + y + 75 + 60 = 360^\circ</math>  <math>2y = 220 = 360</math>  <math>y = 70^\circ</math></p>	<p>9. <math>f(4) = 3(4) + 2</math>  <math>= 12 + 2 = 14</math>  <math>g(14) = 3(14 + 2)</math>  <math>= 48</math></p>	
<p>13. Let (x,y) be any point on the line, then the gradient = <math>\frac{y-9}{x-1}</math>  But gradient is given as 5, so <math>\frac{y-9}{x-1} = 5</math>  <math>y - 9 = 5(x - 1)</math>  <math>y = 5x + 4</math>  Equation of the line is <math>y = 5x + 4</math></p>	<p>14. <math>\frac{1}{3}x - (x + 1) \geq 2</math>  <math>\frac{1}{3}x - x - 1 \geq 2</math>  <math>x - 3x - 3 \geq 6</math>  <math>-2x \geq 9</math>  <math>x \leq \frac{9}{2}</math></p>	<p>12. <math>8x + y = 21</math>   <math>\times 4 \dots(i)</math>  <math>5x - 4y = -10</math>   <math>\times 1 \dots(ii)</math>  <math>32x + 4y = 84</math>  <math>5x - 4y = -10</math>  <math>37x = 74, x = 2</math>  Substitute x in equation (i)  <math>8 \times 2 + y = 21</math>  <math>y = 21 - 16</math>  <math>y = 5</math></p>	
<p>13. Let (x,y) be any point on the line, then the gradient = <math>\frac{y-9}{x-1}</math>  But gradient is given as 5, so <math>\frac{y-9}{x-1} = 5</math>  <math>y - 9 = 5(x - 1)</math>  <math>y = 5x + 4</math>  Equation of the line is <math>y = 5x + 4</math></p>	<p>14. <math>\frac{1}{3}x - (x + 1) \geq 2</math>  <math>\frac{1}{3}x - x - 1 \geq 2</math>  <math>x - 3x - 3 \geq 6</math>  <math>-2x \geq 9</math>  <math>x \leq \frac{9}{2}</math></p>	<p>15. let the number who like both subjects be x,  - then who like maths only = <math>40 - x</math>  - those who like science only = <math>25 - x</math>  So, <math>40 - x + x + 25 - x + 2 = 50</math>  <math>67 - x = 50</math>  <math>x = 17</math>  17 students like both mathematics and science.</p>	

**SECTION B**

16.  $p(x) = 6x^3 - 5x^2 - 12x - 4$

-4 can be a product of -1, 1, 4 or 2, -2, 1

Try  $x - 2$  as a factor  $p(x)$ , then

$p(2) = 6(2)^3 - 5(2)^2 - 12(2) - 4$

so  $x - 2$  is a factor of  $p(x)$

$6x^3 - 5x^2 - 12x - 4$

$\frac{-6x^3 - 12x^2}{-7x^2 - 12x}$

$\frac{7x^2 - 12x}{2x - 4}$

$\frac{2x - 4}{0}$

$\frac{x - 2}{6x^2 + 7x + 2}$

$6x^2 + 7x + 2$   
 $= 6x^2 + 3x + 4x + 2$   
 $= 3x(2x + 1) + 2(2x + 1)$   
 $= (3x + 2)(2x + 1)$

So  $p(x) = (3x + 2)(2x + 1)(x - 2)$

When  $p(x) = 0$ , then  $(3x + 2)(2x + 1)(x - 2) = 0$

$x = -\frac{2}{3}, x = -\frac{1}{2}, x = 2$

17.

a) the curved surface of the cylinder =  $2\pi rh$   
 $= 628\text{cm}^2$

So,  $2(3.14)(10).r = 628$

$r = \frac{628}{62.8}$

$r = 10\text{cm}$

b) The base areas of the cylinder

$= 2\pi r^2$

$= 2 \times 3.14 \times 10^2 = 628\text{cm}^2$

Total surface area of the tin =  $628 + 628$

$= 1256\text{cm}^2$

c) Volume of the tin =  $\pi r^2 h$

$= 3.14 \times 10 \times 10 \times 10$

$= 3140\text{cm}^3$

d) diameter of the tin is 20cm

so along the length, there can be placed  $80 \div 20 = 4$  tins

along the width can be placed  $60 \div 20 = 3$  tins

along the height can be placed  $40 \div 10 = 4$  tins

therefore, the number of tins to fill the box

$= 4 \times 3 \times 4 = 48$  tins

18. a)

Age (x)	Frequency, f	f(x)	Cumulative frequency
14	5	70	5
15	9	135	14
16	13	208	27
17	11	187	38
18	12	216	50
19	15	285	65
20	8	160	73
	$\sum f = 73$	$\sum f(x) = 1261$	

b) The mode is 19 years

c) The median is the

$\frac{1}{2} (73 + 1)^{\text{th}}$  age

$= 37^{\text{th}}$  age

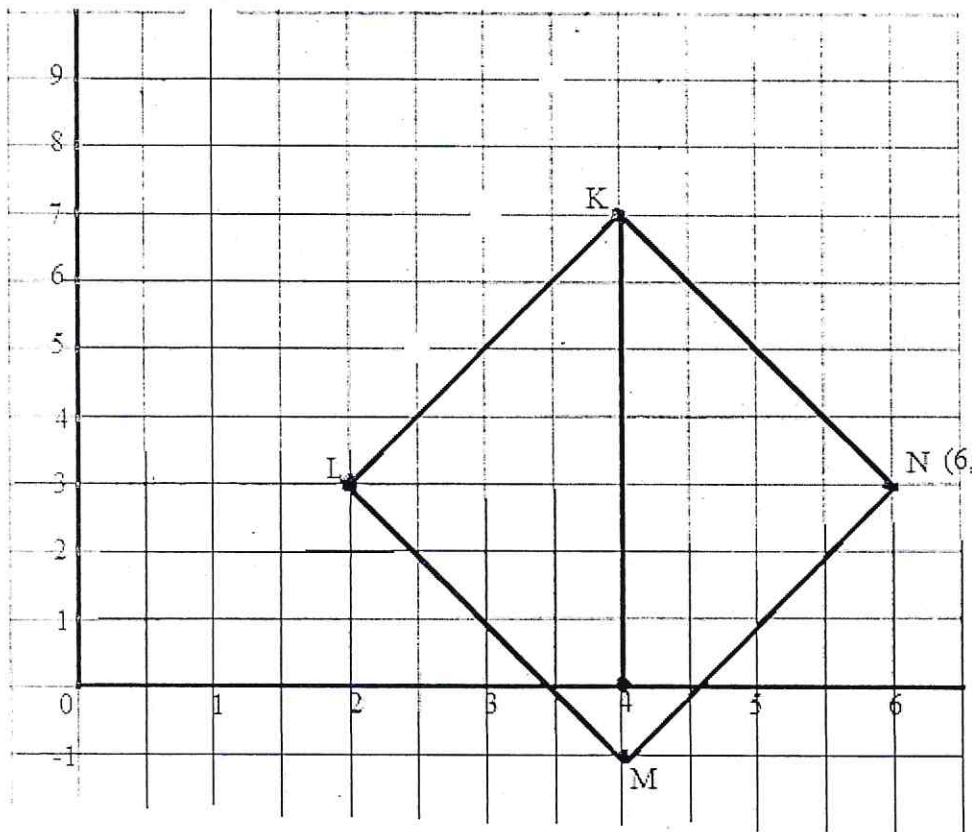
d) The mean age

$= \frac{1261}{73}$

$= 17$  years

<p>19. a) i)</p> $\vec{a} + \vec{b} - \vec{c} = \begin{bmatrix} -5 \\ 12 \end{bmatrix} + \begin{bmatrix} 3 \\ 6 \end{bmatrix} - \begin{bmatrix} -4 \\ -2 \end{bmatrix} = \begin{bmatrix} 2 \\ 20 \end{bmatrix}$	<p>ii) <math>\vec{a} = \sqrt{(-5)^2 + 12^2}</math>  <math>= \sqrt{169}</math>  <math>= 13</math></p>	<p>19. d)</p> <p><math>\vec{s}</math> is parallel to <math>\vec{t}</math>, then</p> $t = k\vec{s}$ $3k = 21$ $k = 3$ $t = \begin{bmatrix} 21 \\ r \end{bmatrix} = 3 \begin{bmatrix} 7 \\ 4 \end{bmatrix}$ $r = 3 \times 4 = 12$
<p>b) i) <math>\vec{KL} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} - \begin{bmatrix} 3 \\ 6 \end{bmatrix} = \begin{bmatrix} -2 \\ -4 \end{bmatrix}</math></p> $ \vec{KL}  = \sqrt{(-2)^2 + (-4)^2} = \sqrt{20} = 2\sqrt{5}$ $\vec{LM} = \begin{bmatrix} 4 \\ -1 \end{bmatrix} - \begin{bmatrix} 2 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ -4 \end{bmatrix}$ $ \vec{LM}  = \sqrt{2^2 + (-4)^2} = \sqrt{20} = 2\sqrt{5}$	<p>19. c) <math>\vec{PQ} = \vec{OQ} - \vec{OP}</math></p> $= \begin{bmatrix} 3 \\ 1 \end{bmatrix} - \begin{bmatrix} -3 \\ -2 \end{bmatrix} = \begin{bmatrix} 6 \\ 3 \end{bmatrix}$ $= \vec{QR} = \vec{OR} - \vec{OQ}$ $= \begin{bmatrix} 5 \\ 2 \end{bmatrix} - \begin{bmatrix} 3 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ $= \vec{PQ} = 3\vec{QR}$ <p>Q is common, therefore P, Q, R are collinear</p>	

b) ii)



20. Teacher's guidance